

Performance Evaluation of OFDM and Modulation Techniques in Mobile WiMAX (IEEE 802.16e)

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Dedication

....To My Family

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ABSTRACT

Mobile communication has developed very during the last few years. Due to this fast development in this field, subscribers of today are enjoying the use of many applications ranging from data, voice, audio to video irrespective of the place where they are stationed or moving about.

WiMAX technology is fast capturing the market in the field of mobile broadband access. WiMAX uses Orthogonal Frequency Division Multiple Access (OFDMA) at the physical layer. WiMAX uses an adaptive modulation technique to modulate the signal prior to transmitting it. Under adaptive modulation, BPSK, QPSK, 16-QAM and 64 QAM are used for modulating the data depending on the channel conditions.

Cyclic Prefix is used to improve the quality of the signal under hostile environments especially Rayleigh fading. Cyclic prefix adds bits to the start and end of data stream to spread the signal. The receiver removes the bits added prior to further processing of the signal. Cyclic prefixing improves the error performance of signals by minimizing Inter Symbol Interference (ISI).

This study focused on the performance of the WiMAX system in terms of Bit Error Rate (BER), Signal to Noise Ratio (SNR), Power Spectral Density (PSD) and Probability of Error (Pe). Two models namely one without the Cyclic Prefix and the other with the Cyclic prefix were built to study these parameters. On analyzing the results, it was observed that adding cyclic prefix improved the error performance marginally especially when the signal is BPSK modulated. The results of BER vs SNR and Pe vs SNR are different as Pe is the expected value of BER where BER approaches Pe when the simulation is run for a long period of

time and the BER is very high. Other situations, Pe and BER show different results under same conditions.

Finally based on the evaluation and conclusion, recommendations were made for further work.

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List of Abbreviations

3GPP	-	3rd Generation Partnership Project
AAA	-	Authentication, Authorization and Accounting
AM	-	Amplitude Modulation
ASK	-	Amplitude Shift Keying
ASN-GW	-	Access Service Network Gateways
ASP	-	Application Service Provider
AWGN	-	Additive White Gaussian Noise
BER	-	Bit Error Rate
BPSK	-	Binary Phase Shift Keying
BS	-	Base Station
BWA	-	Broadband Wireless Access
CC	-	Convolution Code
CEPT	-	European Conference of Postal and Telecommunications Administrations
CSN	-	Connectivity Service Network
DAA	-	Detect and Avoid
DL	-	Downlink
DoS	-	Denial of Service
DPSK	-	Differential Phase Shift Keying
DSL	-	Digital Subscriber Line
DUR	-	Downlink to Uplink Ratio
ETSI	-	European Telecommunication Standard Institute
ECC	-	Electronic Communications Committee

FDM	-	Frequency Division Multiplexing
FDMA	-	Frequency Division Multiple Access
FEC	-	Forward Error Correction
FFT	-	Fast Fourier Transform
FM	-	Frequency Modulation
FSK	-	Frequency Shift Keying
GW	-	Gateway
HAP	-	High Altitude Platform
HiperMAN	-	High Performance Radio Metropolitan Area Network
IEEE	-	Institute of Electrical and Electronic Engineers
IFFT	-	Inverse Fast Fourier Transform
IMS	-	IP Multimedia Subsystem
IP	-	Internet Protocol
ISI	-	Inter Symbol Interference
ITU	-	International Telecommunication Union
LOS	-	Line of Sight
LTE	-	Long Term Evaluation
MAC	-	Media Access Control
MB-OFDM	-	Multiband OFDM
MFSK	-	Multiple Frequency Shift Keying
MGF	-	Moment Generating Function
MPSK	-	Multilevel Phase Shift Keying
MS	-	Mobile Station
MTRNG	-	Mersenne Twister Random Number Generator
NSP	-	Network Service Provider

NWG	-	Network Group
OECD	-	Organization for Economic Co-operation and Development
OFDM	-	Orthogonal Frequency Division Multiplexing
OFDMA	-	Orthogonal Frequency Division Multiple Access
PAPR	-	Peak-to-Average Power Ratio
P_e	-	Probability of Error
PSD	-	Power Spectral Density
PSK	-	Phase Shift Keying
PSTN	-	Public Switched Telephone Network
QAM	-	Quadrature Amplitude Modulation
QoS	-	Quality of Service
QPSK	-	Quadrature Phase Shift Keying
SNR	-	Signal to Noise Ratio
RNG	-	Random Number Generator
RS	-	Reed-Solomon
TDMA	-	Time Division Multiple Access
UP	-	Uplink
WiFi	-	Wireless Fidelity
WiMAX	-	Worldwide Interoperability for Microwave Access
WLAN	-	Wireless Local Area Network
WMAN	-	Wireless Metropolitan Area Network

CHAPTER 1: Introduction

1.0 Background

The telecommunication industry is facing unprecedented competition due to rapid changes in technology [1]. Customers also demand high levels of services from the service providers. The telecommunication service providers try new ways to meet customer demands and add value to their existing products and services using new technologies to gain competitive advantage and to increase customer loyalty.

Wireless technologies are used for many different applications today. Communication is one such industry where wireless technologies are heavily used. The telecommunication industry uses many wireless technologies ranging from fixed wireless to cellular mobile technologies. Worldwide Interoperability for Microwave Access or WiMAX in short is a telecommunication protocol or technology that has captured the attention of both the service providers and customers due to its ability to carry high speed data in a fixed or mobile wireless environment.

ITU, the United Nations specialized agency for telecommunications, is committed to playing a positive role in the development of the information society and to extending the benefits of advances in telephony and new information and communication technologies (ICT), such as broadband, broadband is expected to be one of the highlights of this year's show[3]. For the purpose of monitoring the growth of broadband uptake, as well as in the interest of consumers, each country needs to

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REFERENCES

- [1] Hsiao, I.P.T, "Growth Strategies for Wireless Mobile Service Providers," M.S Thesis., Massachusetts Institute of Technology., Sloan School of Management., 1998.
- [2] Telecom Regulatory Authority of India, "Broadband India: Accelerating Growth of Internet," [online document], 2005 [2010 June 11], Available: http://ldt.stanford.edu/~educ39105/paul/articles_2005/International%20Perspectives/Broadband%20India.pdf
- [3] ITU. " Foreword to the 2003 ITU Internet Report: Birth of Broadband." [online document], 2003 [accessed October 5, 2010], Available : http://www.itu.int/osg/spu/publications/sales/birthofbroadband/exec_summary.html
- [4] LigatureSoft, "Data Transmission Impairments," [Online document], [2010 June 06] Available: http://www.ligaturesoft.com/data_communications/trans-impairment.html
- [5] Horak, R. *Communication Systems and Networks*, Wiley-Dreamtech India Pvt. Ltd., 2002.
- [6] Rhoton, J., *The Wireless Internet Explained*. Digital Press, 2002.
- [7] Pahlavan, K. and Krishnamurthy, P., *Principles of Wireless Networks*, Prentice Hall, Englewood Cliffs, NJ, 2002
- [8] Andrews, J.G, Ghosh, A, Muhamed, R, *Fundamentals of WiMAX: Understanding Broadband Wireless Networking*, Prentice Hall, New Jersey, USA, 2007.
- [9] WiMAX.com, "WiMAX Reference Architecture," [Online document], [2010 June 02], Available: http://www.wimax.com/commentary/wimax_weekly/2-6-reference-network-architecturecontin.
- [10] Stallings, W, "Wireless: Communications and Networks," Pearson Education, New Jersey, USA, 2002.
- [11] Lawrey. E, "The Suitability of OFDM as a Modulation Technique for Wireless Telecommunications, with a CDMA Comparison," MSc Dissertation., James Cook University., Queensland, Australia, 1997.

- [12] Cooper, G.R, Nettleton, R.W, "A spread spectrum technique for high capacity mobile communications", *IEEE Transaction on Vehicular Technology*, Vol. 27, No 4, pp. 264-275,1978.
- [13] Langton. C, "Ine Gtuitivuide to Principles of Communications: OFDM", [Online document], [Accessed: 2010,June07th,], Available: <http://www.complextoreal.com/>
- [14] Ahson, S, Ilyas, M. "WiMAX Technologies," in *Performance Analysis and QoS*, CRC Press , 2004.
- [15] Yin, H, Alamouti, S, "OFDMA: A Broadband Wireless Access Technology", *IEEE Sarnoff Symposium Conf*, 2006, pp. 1 - 4
- [16] Morelli, M, Kuo, C.C.J, Pun, M.O, , "Synchronization Techniques for Orthogonal Frequency Division Multiple Access (OFDMA): A Tutorial Review," *Proceedings of the IEEE Journal of Communications*, Vol. 95, Issue 7, pp. 1394 – 1427, 2007.
- [17] Gurari, E, "Transmission Impairments", Course Notes, Ohio State University, [Online Document], 1998, [2010 June 07], Available: <http://www.cse.ohiostate.edu/~gurari/course/cis677/cis677Se5.html>
- [18] Stallings. W, "Wireless: Communications and Networks", Pearson Education, New Jersey, USA, 2002.
- [19] *Wireless Communications & Networks*, 2nd Edition, Stalling, W. Prentice Hall, New Jersey, USA, 2005.
- [20] *.Wireless Communications: Principles & Practice*, 2nd Edition, Prentice Hall, Rappaport, T.S., New Jersey, USA, 2001.
- [21] Hoffer, J. A, George, J, & Valacich, J, "Modern Systems Analysis and Design", Prentice Hall, New Jersey, USA , 2002.
- [22] Porcino, D, Hirt, W, "Ultra-Wideband Radio Technology: Potential and Challenges Ahead," *IEEE Communications Magazine*, Vol. 41, No. 7, pp. 66–74, July 2003.
- [23] IEEE, "IEEE std 802.16-2004, IEEE Standard for Local and metropolitan area networks Part 16: Air Interface for Fixed Broadband Wireless Access", Institute of Electrical and Electronic Engineers, Inc., USA, 2004.

- [24] Cano, E, Rabbachin, A, Fuehrer, D, Fortuny, J "On the Evaluation of MB-OFDM UWB Interference Effects on a WiMAX Receiver," *EURASIP Journal on Wireless Communications and Networking*, Volume 2008, 2008.
- [25] Li, J, Haggman, S.G, "Performance of IEEE802.16-2004 Based System in Jamming Environment and its Improvement with Link Adaptation," *17th Int IEEE Symposium on Personal, Indoor and Mobile Radio Communications*, Helsinki, Finland, 2006.
- [26] Sklar, B, "Part I: Characterization," in *Rayleigh Fading Channels in Mobile Digital Communication Systems*", *IEEE Communications Magazine*, pp. 90 – 100, 1997.
- [27] IEEE, "IEEE std 802.16e-2005, Amendment to IEEE Standard for Local and metropolitan area networks Part 16: Air Interface for Fixed Broadband Wireless Access Systems – Physical and Medium Access Control Layers for Combined Fixed and Mobile Operation in Licensed Bands," The Institute of Electrical and Electronic Engineers, Inc., USA , 2006.
- [28] Murphy, L, Noonan, J, Perry, P, Murphy, J, "An Application-quality-based Mobility Management Scheme," *9th IFIP International Conference on Mobile Wireless Communications Networks*, Cork, Ireland, 2007.
- [29] Schuerger, J, Garmatyuk, D, "Multifrequency OFDM SAR in Presence of Deception Jamming", *EURASIP Journal on Advances in Signal Processing*, 2010.
- [30] Marey, M, Steendam, H, "Cancellation of Digital Narrowband Interference for Multicarrier Systems," *6th International Workshop on Multicarrier Spread Spectrum, MC-SS'07*, Herrsching, Germany, pp. 127-136, 2007.
- [31] Marey, M, Guenach, M, Steendam, H, "Soft Information Aided Phase Noise Correction for OFDM Systems", *12th International OFDM-Workshop 2007 (InOWo'07)*, Hamburg, Germany, pp. 186-190, 2007.
- [32] Hou, Y, Hase. T, "New OFDM system without guard interval", *Int Consumer Electronic Conf*, Las Vegas, USA, 2009.
- [33] Minn, H, Bhargava, V.K, "An Investigation into Time-Domain Approach for OFDM Channel Estimation," *IEEE Transactions on Broadcasting*, Vol. 46, No. 4, pp. 240-248, 2000.
- [34] Li. Z, "Automatic Detection of the Guard Interval Length in OFDM System," *Journal of Communications*, Vol. 1, No. 6, pp. 29-32, 2006.

- [35] Steendam, H, Moeneclacy, M, "Different Guard Interval Techniques for OFDM: Performance Comparison," *6th Int Workshop on Multicarrier Spread Spectrum, MC-SS'07*, Herrsching, Germany, pp. 11-24, 2007.
- [36] Agilent, "An Introduction in *Digital Modulation*," in *Communications Systems*, Application Note 1298, Agilent Technologies, USA, 2001.
- [37] Wymeersch, H.; Steendam, H.; Moeneclacy, M.; , "Interleaved coded modulation for non-binary codes: a factor graph approach," *Global Telecommunications Conference, 2004. GLOBECOM '04. IEEE* , vol.1, no., pp. 525- 529 Vol.1, 29 Nov.-3 Dec. 2004
- [38] *Digital Communications: Fundamentals and Applications*, Prentice Hall, Sklar. B, Upper Saddle River, NJ, USA, 2001.
- [39] Seok-Jun Lee; Goel, M.; Zhu, Y.; Jing-Fei Ren; Yang Sun; , "Forward error correction decoding for WiMAX and 3GPP LTE modems," *Signals, Systems and Computers, 2008 42nd Asilomar Conference on* , vol., no., pp.1143-1147, 26-29 Oct. 2008
- [40] Jin Jin; Baochun Li; , "Adaptive Random Network Coding in WiMAX," *Communications, 2008. ICC '08. IEEE International Conference on* , vol., no., pp.2576-2580, 19-23 May 2008
- [41] Jin Jin; Baochun Li; Taegon Kong; , "Is Random Network Coding Helpful in WiMAX?," *INFOCOM 2008. The 27th Conference on Computer Communications. IEEE* , vol., no., pp.2162-2170, 13-18 April 2008
- [42] Beitmashal, E, Ashourian, M, Kazemi, H, "Adaptive Modulation and Coding in WiMAX System for Optimum Image Transmission", *Innovative Technologies in Intelligent Systems and Industrial Applications Conf*, Monash, Australia, 2009.
- [43] Jin, J, Li, B, "Cooperative Multicast Scheduling with Random Network Coding in WiMAX," *17th International Workshop on Quality of Service, IWQoS*, Charleston, SC, USA, 2009.
- [44] WWW, (2010), "RF System and Circuit Challenges for WiMAX," [Online document], 2010, [2010 may 13], Available: http://www.intel.com/technology/itj/2004/volume08issue03/art02_rfssystem/p05_wimax_specs.htm.

- [45] Liu, Y.H, Chen, H.C, Wang, T, Lu, S.S, "A CMOS transmitter front-end with digital power control for WiMAX 802.16e applications," *Asia-Pacific Microwave Conf*, Yokohama, Japan, 2005.
- [46] Sanchez-Gaspariano, L.A, Diaz-Sanchez, A, "IEEE 802.16e Design Issues and Transceiver Architecture Selection for Mobile WiMAX Systems", *18th Int Electronics, Communications and Computers Conf*, Puebla, Mexico, 2008.
- [47] Fukao, C, Kogane, R, Itami, M, itoh, K, "Detection of WiMAX signal using Guard Interval Correlation in MB-OFDM," In Proc , Institute of Electronic, Information and Communication Engineers, Ibaraki, Japan, 2007.
- [48] ECC, "Technical Requirements for UWB DAA (Detect and Avoid) Devices to Ensure the Protection of Radiolocation Services in the Bands 3.1 - 3.4 GHz And 8.5 - 9 GHz and BWA Terminals in the Band 3.4 - 4.2 GHz", ECC Report 120, Electronic Communications Committee (ECC), *Postal and Telecommunications Administrations (CEPT) European Conf* , Kristiansand, Germany, 2008.
- [49] Park, J.H; Ban, M; Cho, S.H, (2008), "A Design of a Mobile WiMAX System for Military Applications and its Performance in Fading Channels," *Int Advanced Technologies for Communications Conf*, Hanoi, Vietnam, 2008.
- [50] WiMAX , "Mobile WiMAX – Part I: A Technical Overview and Performance Evaluation" in WiMAX Online discussion Forum 2006, San Diego, CA, USA.
- [51] Simon, M.K, Alouini, M.S, "A Unified Approach to the Probability of Error for Non-coherent and Differentially Coherent Modulations over Generalized Fading Channels," *IEEE Transactions on Communications*, Vol. 46, pp. 1625-1638, 1998.
- [52] Nakagami, M, "The m-distribution – A General Formula of Intensity Distribution of Rapid Fading," in *W.G Hoffman Statistical Methods in Radio Wave Propagation*, Pergamon, 1960.
- [53] Alouini, M.S, Simon, M.K, "Multichannel Reception of Digital Signals over Correlated Nakagami Fading Channels," *IEEE Transactions on Communications*, Vol. 86, pp. 1860-1877, 1998.
- [54] Braun W.R, Dersch, U, "A Physical Mobile Radio Channel Model," *IEEE Trans. on Vehicular Technology*, Vol. 40, pp. 472-482, 1991.

- [55] Hashemi, H, "The Indoor Radio Propagation Channel," *Proc. IEEE*, Vol. 81, pp. 943-968, 1993.
- [56] Kothari. S, "Adoption of B2B e-commerce by SMEs", *Journal of Accounting and Economics*, 1995.
- [57] Matsumoto, M, Nishimura, T, "Mersenne Twister: A 623-Dimensionally Equidistributed Uniform Pseudo-Random Number Generator", *ACM Transactions on Modeling and Computer Simulation*, Vol. 8, No. 1, 1998, pp. 3–30.
- [58] Saito, M, Matsumoto, M, "SIMD-oriented Fast Mersenne Twister: a 128-bit Pseudorandom Number Generator," in *Monte Carlo and Quasi-Monte Carlo Methods 2006*, 2008, Springer Publications, pp. 607